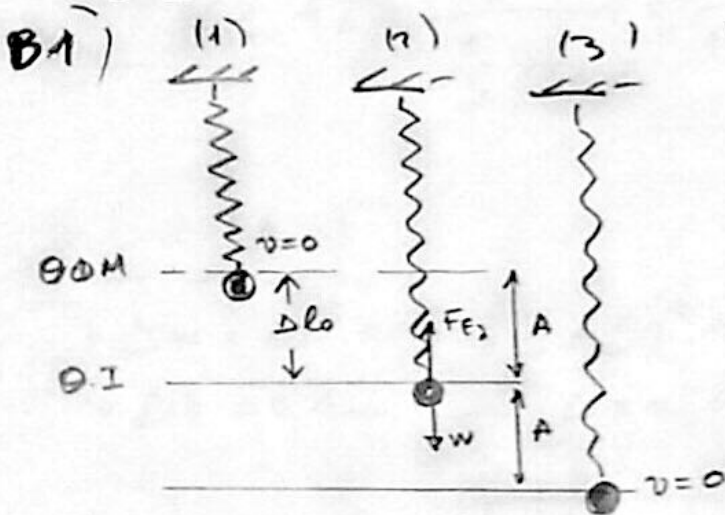


● ΘΕΜΑ Α.

A1) δ , A2) γ , A3) α , A4) δ , A5) λ, ς, ς, ς, λ

● ΘΕΜΑ Β



• Ισορροπία (2): $\sum F_y = 0 \Rightarrow F_{e2} = W \Rightarrow$
 $\Rightarrow k \Delta l_0 = mg \Rightarrow \Delta l_0 = \frac{mg}{k}$

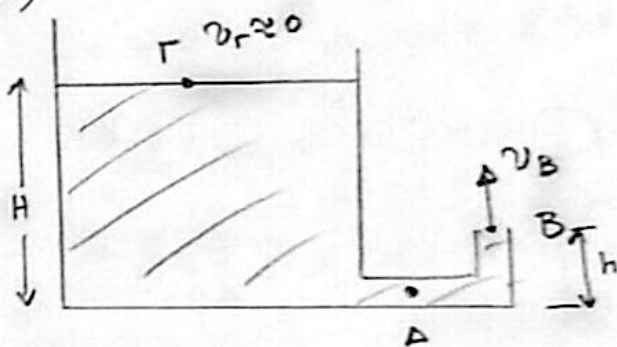
• Έτσι $A = \Delta l_0$

• $v_{e2(max)} = \frac{1}{2} k \Delta l_{max}^2 \Rightarrow$

• $\Delta l_{max} = 2A$

$\Rightarrow v_{e2(max)} = \frac{2m^2 g^2}{k}$ (ii)

B.2)



• Από θεωρία Torricelli, προκύπτει ότι: $v_B = \sqrt{2g(H-h)}$

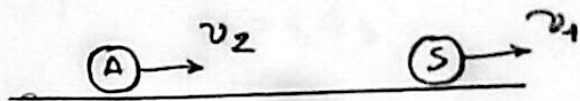
$\Rightarrow v_B = \sqrt{2g(5h-h)} = \sqrt{2g \cdot 4h} \Rightarrow$

$\Rightarrow v_B = 2 \cdot \sqrt{2gh}$ (i)

• Εξίσωση συνέχειας: $A_A \cdot v_A = A_B \cdot v_B \Rightarrow v_A = v_B \Rightarrow$

$\Rightarrow v_A = 2 \cdot \sqrt{2gh}$ (iii)

B.3)



• Eivar. $f_A = \frac{v_{Hx} + v_2}{v_{Hx} + v_1} \cdot f_s = \frac{v_{Hx} + \frac{v_{Hx}}{10}}{v_{Hx} + \frac{v_{Hx}}{5}} \cdot f_s \Rightarrow$

$\Rightarrow f_A = \frac{\frac{11}{10} v_{Hx}}{\frac{6}{5} v_{Hx}} f_s = \frac{5 \cdot 11}{10 \cdot 6} f_s \Rightarrow \boxed{f_A = \frac{11}{12} f_s} \quad (ii)$

• ΘEMA Γ

• $\Delta m = 10^{-6} \text{ kg}$, $E = 5\pi^2 \cdot 10^{-7} \text{ J}$.

• $\Delta t = 0,4 \text{ m} \rightarrow \Delta x = 4 \text{ cm}$

Γ.1) • $\Delta t = \frac{T}{2} \Rightarrow \boxed{T = 0,8 \text{ s}}$

• $\Delta x = \frac{\lambda}{2} \Rightarrow \boxed{\lambda = 8 \text{ cm}}$

• $\omega = \frac{2\pi}{T} \Rightarrow \omega = 2,5\pi \text{ rad/s}$

• $D = \Delta m \cdot \omega^2 \Rightarrow D = 6,25\pi^2 \cdot 10^{-6} \text{ N/m}$

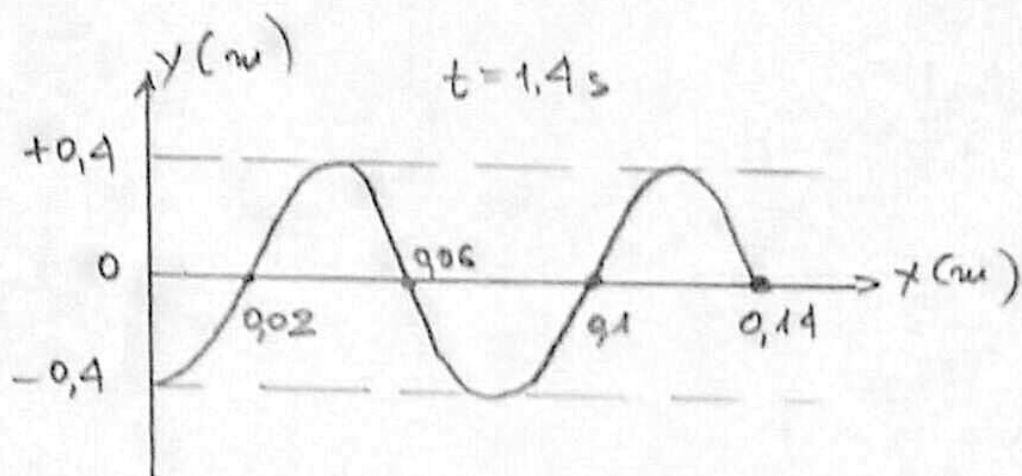
• $E = \frac{1}{2} D A^2 \Rightarrow A = \sqrt{\frac{2E}{D}} \Rightarrow \boxed{A = 0,4 \text{ cm}}$

Γ.2) • $y = A \cdot \mu \cdot 2\pi \left(\frac{t}{T} - \frac{x}{\lambda} \right) \Rightarrow \boxed{y = 0,4 \cdot \mu \cdot 2\pi (1,25t - 12,5x)} \quad (iii)$

• $v_s = \frac{\lambda}{T} \Rightarrow v_s = 0,1 \text{ m/s}$

• $x = v_s \cdot t \Rightarrow x = 0,14 \text{ m}$

• $\frac{x}{\lambda} = \frac{7}{4} \Rightarrow x = 7 \frac{\lambda}{4} \text{ m} \Rightarrow x = 7,25 \text{ m}$



Г.3) $\Delta E_T \quad E = K + U \Rightarrow K = E - U \Rightarrow K = E - \frac{1}{2} D y^2$
 $\Rightarrow K = 5\pi^2 \cdot 10^{-7} - \frac{1}{2} 6,25\pi^2 \cdot 10^{-6} \cdot 4 \cdot 10^{-2} \Rightarrow$
 $\Rightarrow K = 5\pi^2 \cdot 10^{-7} - 1,25\pi^2 \cdot 10^{-2} \Rightarrow \boxed{K = 3,75\pi^2 \cdot 10^{-2}}$

Г.4) $\varphi_P - \varphi_Z = \frac{3\pi}{2} \text{ rad} \Rightarrow \varphi_Z = \varphi_P - \frac{3\pi}{2} \quad (1)$
 $\bullet \quad y_P = 0,4 \text{ m} \mu \varphi_P \Rightarrow 0,4 = 0,4 \text{ m} \mu \varphi_P \Rightarrow \mu \varphi_P = 1 = \mu \mu \frac{\pi}{2} \Rightarrow$
 $\Rightarrow \varphi_P = 2k\pi + \frac{\pi}{2} \quad (2)$
 $(1), (2) \Rightarrow \varphi_Z = 2k\pi + \frac{\pi}{2} - \frac{3\pi}{2} \Rightarrow \varphi_Z = 2k\pi - \pi \quad (3)$
 $\bullet \quad v_Z = \omega A \cdot 6\omega \varphi_Z \Rightarrow v_Z = \pi \cdot 6\omega \varphi_Z \Rightarrow v_Z = \pi \cdot 6\omega (2k\pi - \pi) \Rightarrow$
 $\Rightarrow v_Z = \pi \cdot 6\omega (-\pi) \Rightarrow \boxed{v_Z = -\pi \omega / \text{s}}$

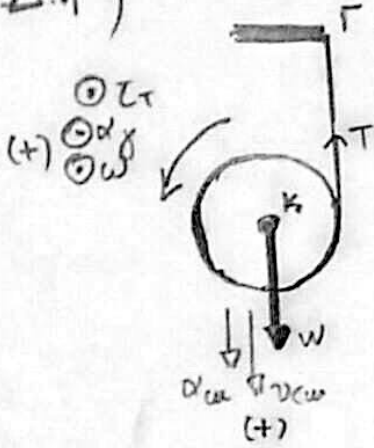
● ΘΕΜΑ Δ.

ΑΓ: $M=4\text{kg}$, φ ,

$g=10\text{m/s}^2$, $\mu\varphi=0,8$
 $6\mu\varphi=9,6$

Δίσκος: $m=2\text{kg}$, $R=0,1\text{m}$, $I_{cm}=\frac{1}{2}mR^2$

Δ.1)



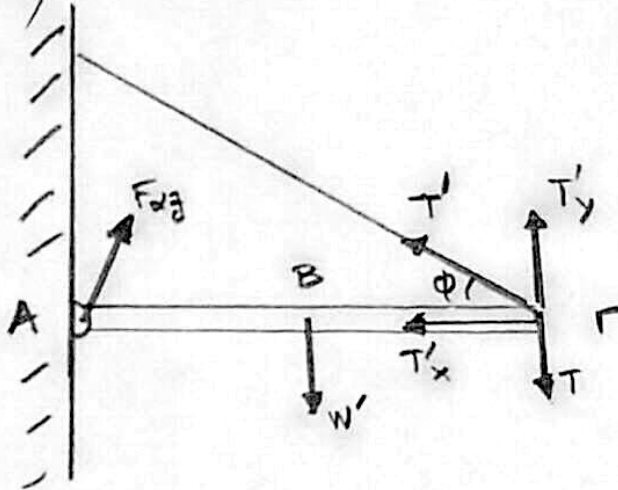
- $\sum F_x = m a_{cm} \Rightarrow mg - T = m a_{cm} \Rightarrow 20 - T = 2 a_{cm} \quad (1)$
- $\sum \tau = I \alpha \Rightarrow T \cdot R = \frac{1}{2} M R^2 \alpha \Rightarrow T = \frac{1}{2} m R \alpha \quad (2)$
- $\alpha_{cm} = \alpha \cdot R \quad (3)$

(2), (3) $\Rightarrow T = \frac{1}{2} m a_{cm} \Rightarrow T = a_{cm} \quad (4)$

(1) + (4) $\Rightarrow 20 = 3 a_{cm} \Rightarrow$

$$a_{cm} = \frac{20}{3} \frac{\text{m}}{\text{s}^2}$$

Δ.2)



(4) $\Rightarrow T = \frac{20}{3} \text{N}$

• $\sum \tau_A = 0 \Rightarrow T'_y \cdot l - T \cdot l - Mg \frac{l}{2} = 0 \Rightarrow$

$\Rightarrow T'_y - \frac{20}{3} - 20 = 0 \Rightarrow$

$\Rightarrow T'_y = \frac{80}{3} \text{N}$

• $T'_y = T' \cdot \mu\varphi \Rightarrow \frac{80}{3} = T' \cdot 0,8 \Rightarrow$

$$T' = \frac{100}{3} \text{N}$$

Δ.3) $h_1 = 0,3\text{m}$, κόβεται το νήμα.

• $h_1 = \frac{1}{2} a_{cm} \Delta t_1^2 \Rightarrow 0,3 = \frac{10}{3} \Delta t_1^2 \Rightarrow \Delta t_1^2 = \frac{0,9}{10} \Rightarrow \Delta t_1 = 0,3 \text{s}$

• $v_{cm(1)} = a_{cm} \Delta t_1 = \frac{20}{3} \cdot 0,3 \Rightarrow v_{cm(1)} = 2 \text{m/s}$

• $v_{cm(1)} = \omega_1 R \Rightarrow 2 = \omega_1 \cdot 0,1 \Rightarrow \omega_1 = 20 \text{rad/s}$

• $L_1 = I \omega_1 = \frac{1}{2} m R^2 \omega_1 = \frac{1}{2} \cdot 2 \cdot 0,01 \cdot 20 \Rightarrow L_1 = 0,2 \text{kg m}^2/\text{s}$

Αφού κοπή το νήμα, $\Sigma \tau = 0 \Rightarrow \text{Α.Δ.Σ} \Rightarrow L = 6\pi\omega\theta$.

Άρα
$$L = 0,2 \text{ kg}\cdot\text{m}^2/\text{s}$$

Δ4) $\Delta t' = 0,1 \text{ s}$

• Αφού κοπή το νήμα, $\omega = 6\pi\omega\theta \Rightarrow \omega = 20 \text{ rad/s}$

• $K_{\text{περ}} = \frac{1}{2} I \omega^2 = \frac{1}{2} \cdot \frac{1}{2} m R^2 \omega^2 = \frac{1}{4} \cdot 2 \cdot 0,01 \cdot 400 \Rightarrow$

$\Rightarrow K_{\text{περ}} = 2 \text{ J}$

• $\Sigma F = m a'_{\text{cm}} \Rightarrow mg = m a'_{\text{cm}} \Rightarrow a'_{\text{cm}} = g = 10 \text{ m/s}^2$

• $v_{\text{cm}} = v_1 + a'_{\text{cm}} \cdot \Delta t' \Rightarrow v_{\text{cm}} = 2 + 10 \cdot 0,1 \Rightarrow v_{\text{cm}} = 3 \text{ m/s}$

• $K_{\text{μετ}} = \frac{1}{2} m v_{\text{cm}}^2 = \frac{1}{2} \cdot 2 \cdot 3^2 \Rightarrow K_{\text{μετ}} = 9 \text{ J}$

• Άρα
$$\frac{K_{\text{περ}}}{K_{\text{μετ}}} = \frac{2}{9}$$